



# Analysis of Learning Map Structure for a Dynamic Assessment

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## Abstract

This study examines the structure of a learning map used for dynamic assessment in grades three through high school. Students were assessed on items measuring 307 nodes, a dramatically larger number of skills when compared with previous diagnostic assessment analyses. Student response data were used to model mastery probabilities at the node level, and these values were used to make recommendations regarding node-to-node connections in the learning map as well as node granularity. These findings were shared with content teams to serve as supporting evidence in their decision-making process for map revisions pertaining to the order and size of cognitive skills.

## Research Purpose

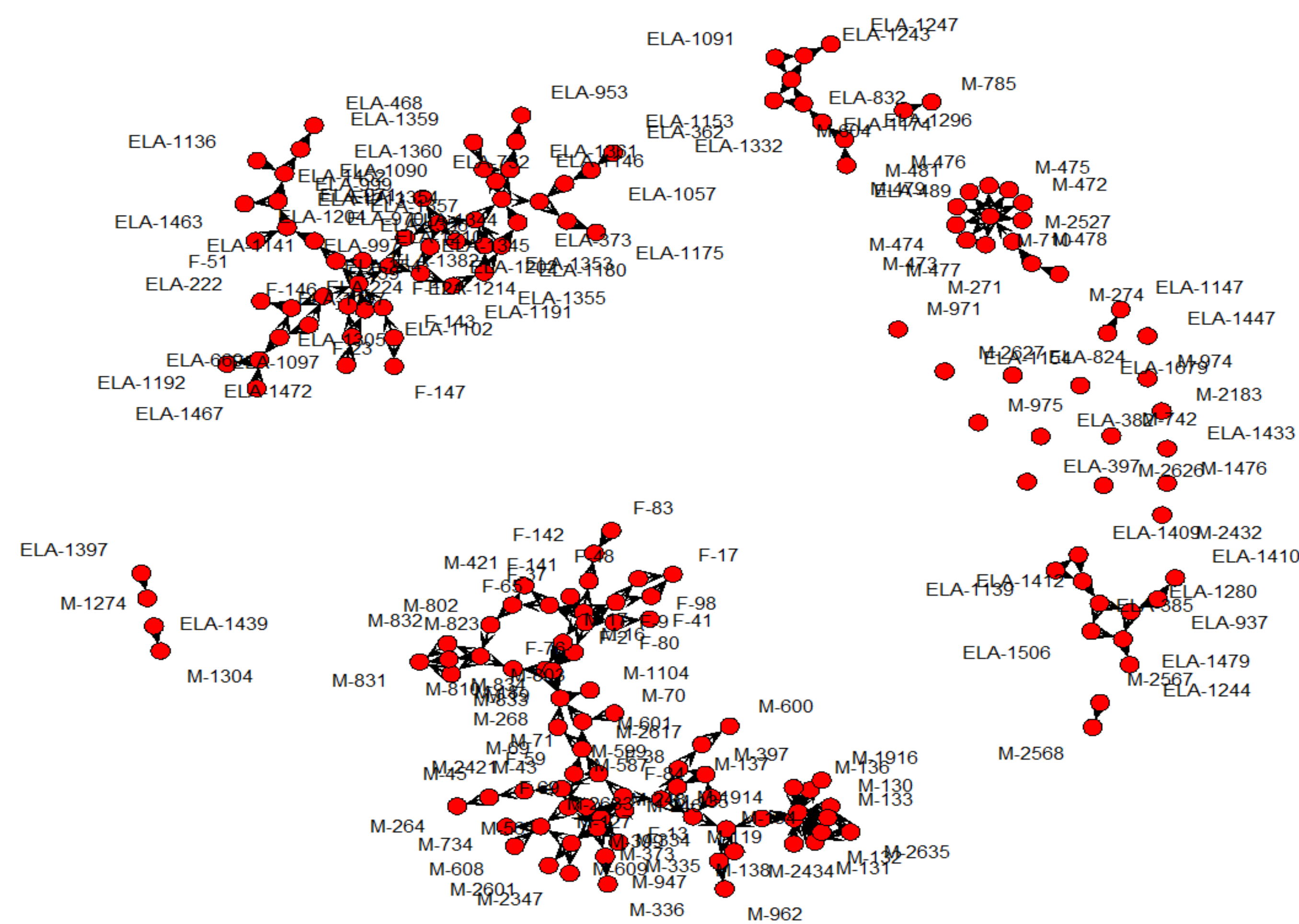
The current study covers three critical analyses in the evaluation of the underlying structure of a learning map used in a dynamic assessment environment.

1. Analysis of the connections between nodes in the learning map
2. Analysis of node granularity in the learning map
3. Content review of statistical recommendations

## Methodology

### Data

- Data came from 22,733 students in grades 3 through 12 across seventeen participating states assessed from spring 2014 to spring 2015
- 1,744 English language arts items
  - Only included items with sample size  $\geq 100$
- 532 English language arts testlets
  - Each testlet consisted of 3 - 8 items
- 214 nodes measured English language arts

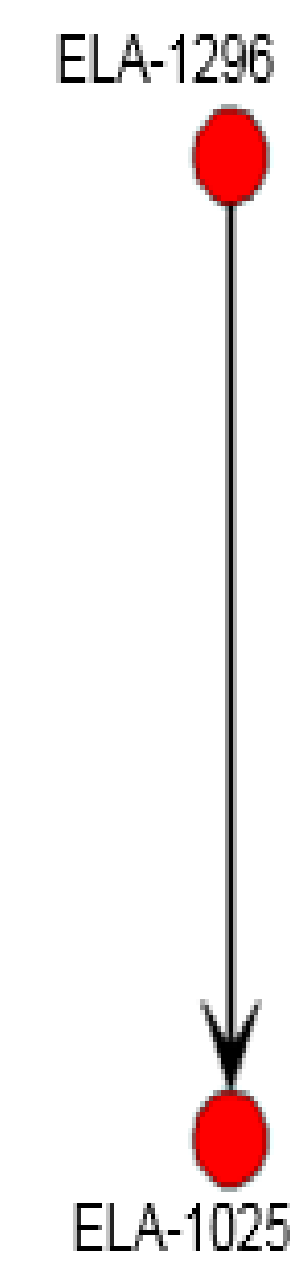


### Modeling

- Bayesian Inference Networks were employed to make causal inferences using conditional probabilities of multiple observations
- Loglinear cognitive diagnosis model (LCDM; Henson, Templin, & Willse, 2009), testlet effect included
- The Metropolis-Hastings algorithm, a Markov Chain Monte Carlo (MCMC) method for obtaining a sequence of random samples from a probability distribution was employed

## Results

### Node-Level Example Results:



Map parameters	Logit	Credible Intervals	Geweke Z	Heidelberger p-value
ELA-1296	-.91	[-1.23, -.47]	5.94	.08
ELA-1025.ELA-1296	1.97	[.09, 4.48]	-5.52	.08
ELA-1025	.37	[-.95, 1.30]	5.38	.13

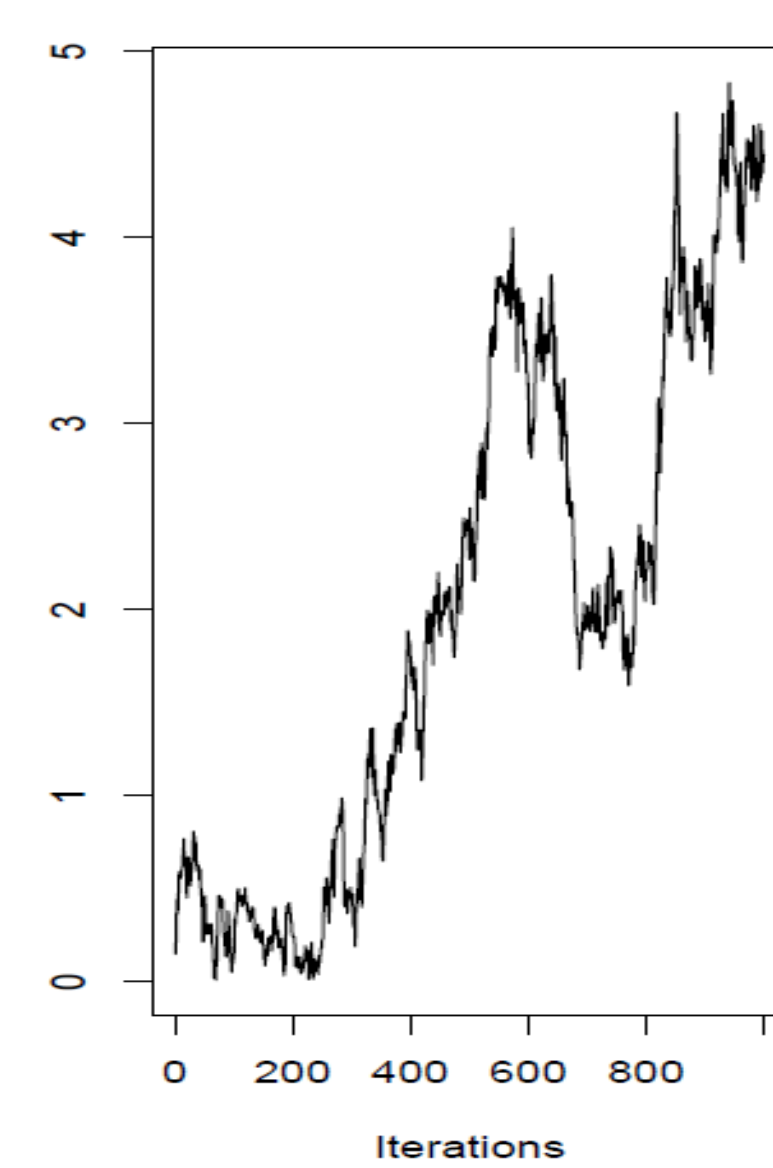
$$P(\alpha_{n_1} = 1) = \frac{\exp(\mu_{n_1,0})}{1 + \exp(\mu_{n_1,0})} \quad \text{Node: ELA-1296}$$

Logit for Master of Node	Master	Non-Master
$\mu_{ELA-1296,0} = -0.911$	.29	.71

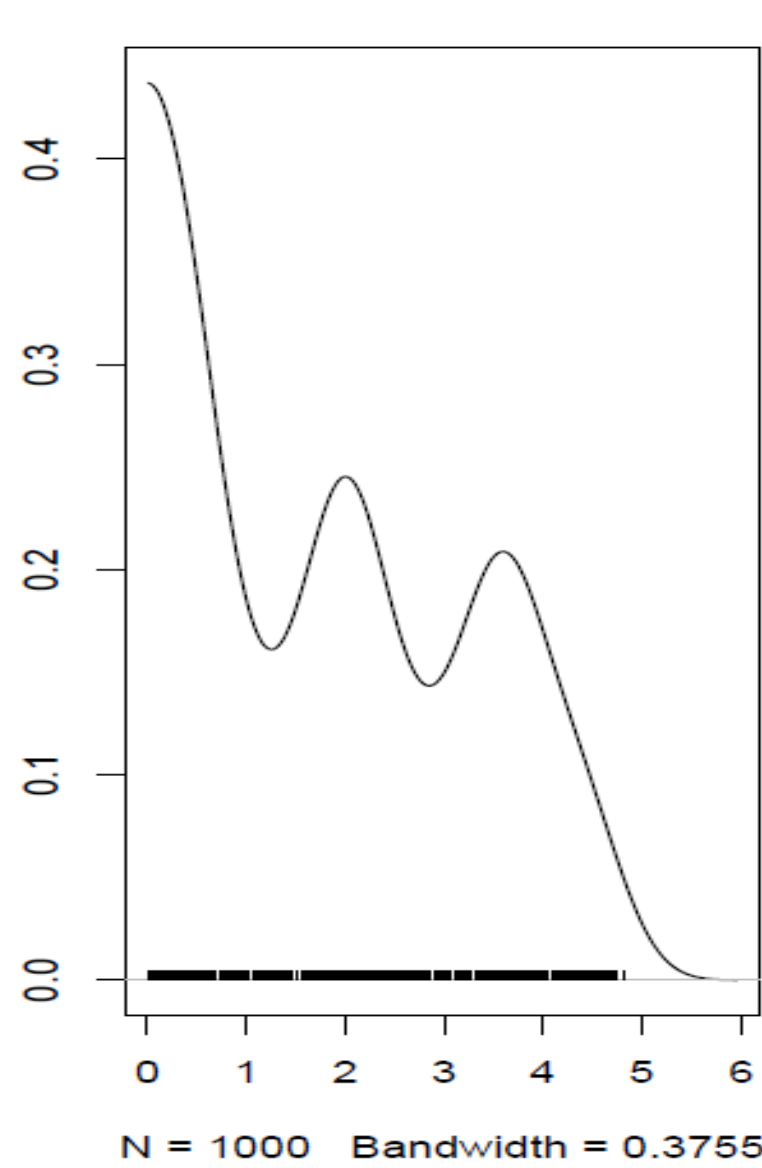
$$P(\alpha_{n_2} = 1 | \alpha_{n_1}) = \frac{\exp(\mu_{n_2,0} + \mu_{n_2,1(n_1)} \alpha_{sn_1})}{1 + \exp(\mu_{n_2,0} + \mu_{n_2,1(n_1)} \alpha_{sn_1})} \quad \text{Node: ELA-1025}$$

Node ELA-1296	Logit for Master of Node ELA-1025	Master	Non-Master
Non-Master	0.37	.59	.41
Master	0.37 + 0.29	.91	.09

Trace of ELA.1025.ELA.1296



Density of ELA.1025.ELA.1296



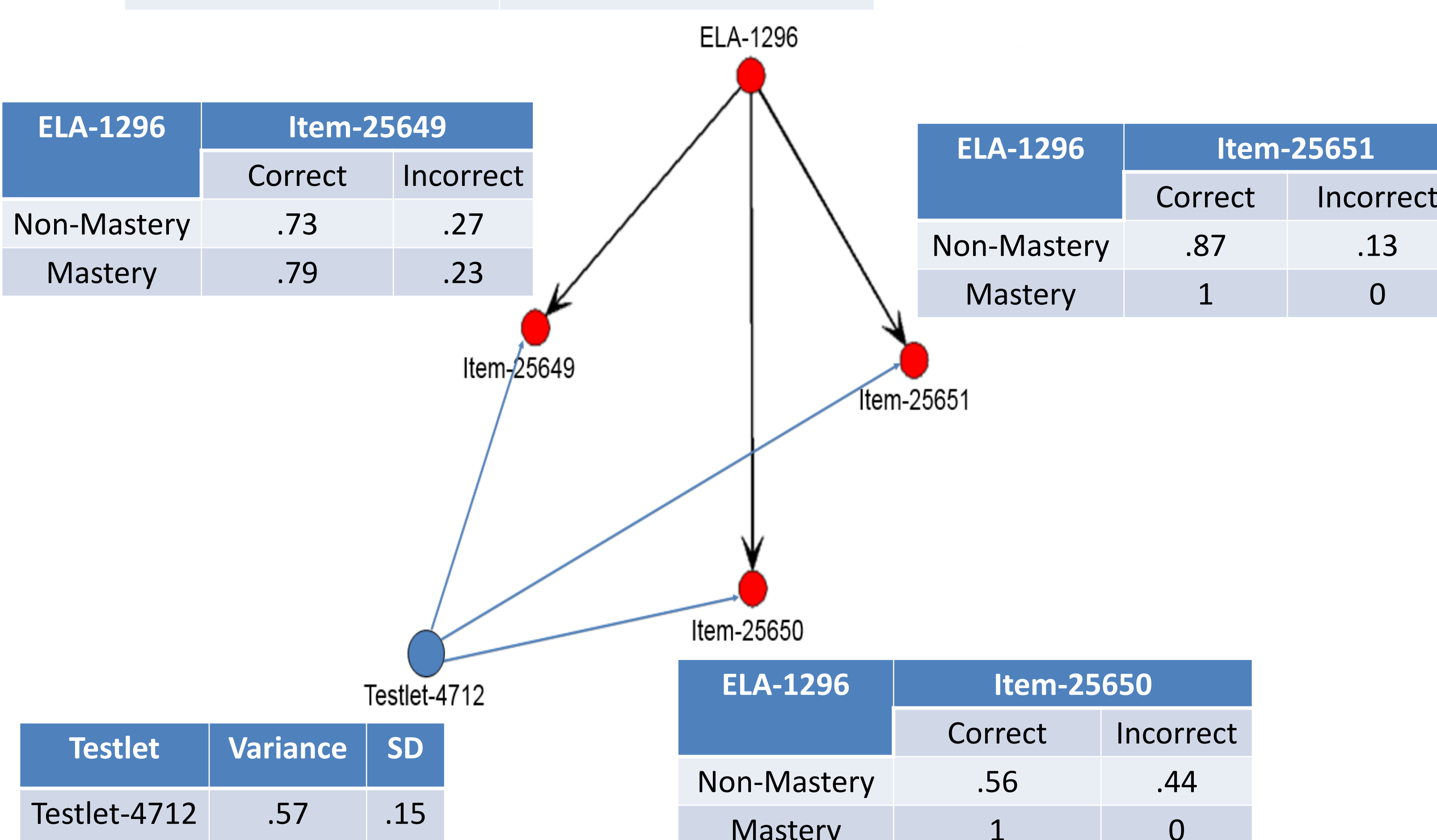
### Item-Level Example Results:

ELA - 1296	
Non-Mastery	Mastery
.29	.71

$$P(Y_{si(t)} = 1 | \alpha_s, \gamma_t) = \frac{\exp(\gamma_t + \lambda_{i(t),1} \alpha_{sa})}{1 + \exp(\gamma_t + \lambda_{i(t),1} \alpha_{sa})}$$

ELA-1296	Item-25649	
	Correct	Incorrect
Non-Mastery	.73	.27
Mastery	.79	.23

ELA-1296	Item-25651	
	Correct	Incorrect
Non-Mastery	.87	.13
Mastery	1	0



Testlet	Variance	SD
Testlet-4712	.57	.15

ELA-1296	Item-25650	
	Correct	Incorrect
Non-Mastery	.56	.44
Mastery	1	0

## Results Continued

Overall convergence rate: 84%

### Node-Level Results:

- Nodes convergence rate: 90%
- Node reversal: nodes where non-masters have a high chance of being master on subsequent nodes
  - Includes intercept value of the successor node greater than zero
  - 46 reversal nodes out of 214 English language arts nodes
- Node overspecification: where two nodes are not distinguishable from one another
  - Includes intercept value less than -4, and main effect value greater than 8
  - No such nodes found satisfying two of the conditions simultaneously

### Item-Level Results:

- Good items: items discriminate well between masters and non-masters of the node
- Non-informative items: items not discriminating, and thus to be flagged
  - 299 out of 1,744 items flagged

## Conclusions

- Based on the results presented, map connections and causal relationships hold in general. There are 46 out of 214 nodes were flagged as potential reversals, which may jeopardize the node connections. Such results could be caused by non-informative items within the nodes, testlet effects in the model, or length of chains being burnt.
- In terms of node granularity, no overspecified nodes were detected among the 214 nodes assessed by items with a sample size of  $\geq 100$ , meaning that all the examined nodes were reasonably distinct from their precursors and did not need to be collapsed.
- In addition to node-level estimation, item-level examination for informing test construction, scoring, quality control, and other features of test development. Items are expected to discriminate well between masters and non-masters of the node. Items that fail to provide such information are to be flagged and reviewed by content experts.
- Statistical evidence provides one source of information for evaluating the structure of the map. Content experts review flags in context of testlet, test specifications, and underlying cognitive processes to make final item quality determinations.

## References

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